Code: ME7T3

IV B.Tech - I Semester – Regular/Supplementary Examinations October - 2018

FINITE ELEMENT METHODS (MECHANICAL ENGINEERING)

Duration: 3 hours

Max. Marks: 70

PART - A

Answer *all* the questions. All questions carry equal marks $11 \ge 22$ M

1.

- a) Differentiate isotropic and orthotropic materials.
- b) State the principle of minimum potential energy.
- c) Discuss penalty approach for handling boundary condition.
- d) Explain the concept of global numbering.
- e) Discuss the different types of loading that act on a structure.
- f) Mention the characteristics of shape function.
- g) Explain about constant strain triangle.
- h) Discuss Jacobian transformation matrix.
- i) Mention the matrix relating the strains and nodal displacements for an axi symmetric triangular element
- j) State the Fourier's law of heat conduction
- k) Explain the governing equations for one dimensional heat conduction

PART - B

Answer any *THREE* questions. All questions carry equal marks. $3 \ge 16 = 48 \text{ M}$

- 2. a) In a plane strain problem, $\sigma_x = 1360$ bar and $\sigma_y = -680$ bar, $\upsilon = 0.3$ and $E = 2 \times 10^6$ bar, find the value of the stress σ_z . 4 M
 - b) Using Rayleigh Ritz method find the displacement at the midpoint of the rod shown in the below Fig 1. 12 M

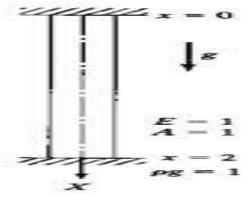
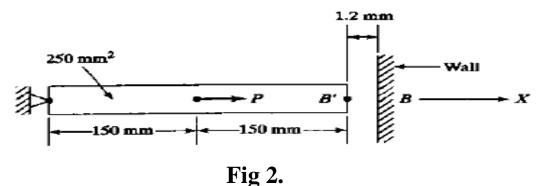


Fig 1.

3. Consider a load of $60 \ge 10^3$ N is applied on the bar shown in the below Fig 2. Determine the displacement field, stress and support reactions in the body. Take E=20 \x 10³ N/mm². 16 M



- 4. Derive the Jacobian matrix for the quadrilateral element with the nodal coordinates (0,0) (10,1) (10,8) and (1,7) for the nodes 1, 2, 3 and 4 respectively. Determine the determinant of the Jacobian at the nodes and at the centroid of the element.
- 5. a) Evaluate the shape functions N_1 , N_2 and N_3 at the interior point P for the triangular element shown in the Fig 3. 8 M

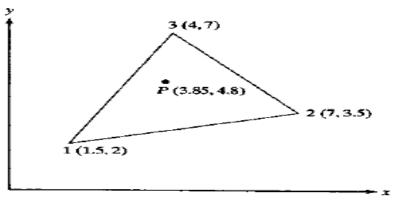


Fig 3.

b) Determine the Jacobian transformation for the element shown in the Fig 4.8 M

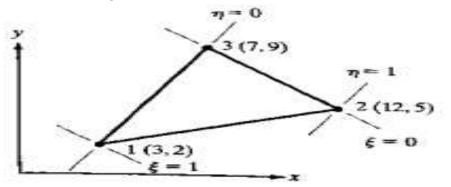


Fig 4.

6. a) An open ended steel cylinder shown in the below
Fig 5. Is subjected to an internal pressure of 5 MPa.
Find the deformed shape and distribution of principal stresses.
10 M

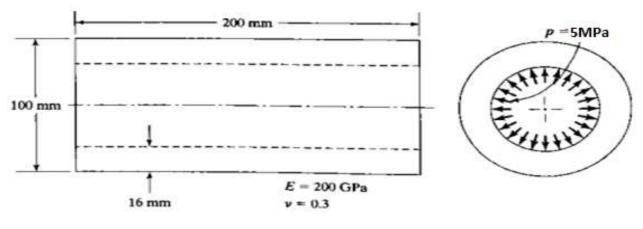


Fig 5.

b) Heat is generated in a large Wall (K = $0.8 \text{ W/m.}^{0}\text{C}$) at the rate of 4000 W/m³. The plate is 25 cm thick. The outside surfaces of the plate is exposed to ambient air at 30^{0}C with a convective heat transfer coefficient of 20 W/m^{2} . Determine the temperature distribution in the wall. 6 M